

LASCON VIII

Tutorials

1. Study the behavior of a plastic synapse described by the Markram-Tsodyks formalism. The synaptic efficacy after the n^{th} spike is proportional to $u_n R_n$. The time evolution is given by:

$$u_{n+1} = u_n \exp(-\Delta t / \tau_{facil}) + U(1 - u_n \exp(-\Delta t / \tau_{facil})) \quad (1)$$

$$R_{n+1} = R_n(1 - u_{n+1}) \exp(-\Delta t / \tau_{rec}) + 1 - \exp(-\Delta t / \tau_{rec}) \quad (2)$$

where Δt is the time between spike n and spike $n + 1$.

- Assuming that the spikes are generated periodically with a period $T = 1/f$, evaluate the synaptic efficacy as a function of f
 - Compare the previous result with the one obtained for a Poisson process with the same average frequency.
 - Explore the space of parameters $U, \tau_{facil}, \tau_{rec}$. Consider de cases $U \ll 1, U \approx 0.5, \tau_{facil} \ll \tau_{rec}, \tau_{facil} \gg \tau_{rec}$
2. Estimate the capacity of the Hopfield model without noise.
 - Create the patterns ξ_i^μ ($i = 1, \dots, N; \mu = 1, \dots, p$). Each one of the values is ± 1 with equal probability.
 - Evaluate the matrix of connections: $J_{ij} = \frac{1}{N} \sum_{\mu=1}^p \xi_i^\mu \xi_j^\mu$ (take $J_{ii} = 0$).
 - Take each one of the patterns as initial condition and iterate until the dynamic converges to a fixed point (s_i^μ).
 - Evaluate the overlap $m^\mu = \frac{1}{N} \sum_{i=1}^N s_i^\mu \xi_i^\mu$.
 - Repeat for all the patterns and evaluate the distribution of overlaps.
 - Repeat for $N = 500, 1000, 2000, 4000$ and $\alpha = p/N = 0.12, 0.14, 0.16, 0.18$
 3. Simulate the dynamics of the Hopfield model with noise using:

$$Pr(s_i(t+1) = \pm 1) = \frac{\exp(\pm \beta h_i(t))}{\exp(\beta h_i(t)) + \exp(-\beta h_i(t))} \quad (3)$$

where $h_i(t) = \sum_{j=1}^N J_{ij} s_j(t)$. Take as initial condition each one of the patterns (ξ_i^μ) . Apply the rule and after visiting each site 10 times evaluate the overlap. Take $N = 4000, p = 40$ and plot the average overlap as a function of $T = 1/\beta$, for $T = 0.1, 0.2, \dots, 2$.